

# Generating None-Plans in Order to Find Plans

Michał Knapik\*

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\*a joint work with Wojciech Penczek and Artur Niewiadomski

# Outline

- 1 Introduction
- 2 Planning in PlanICS
- 3 Simplified Planning Domain
- 4 Plans and None-plans
- 5 Synthesis of None-Plans
- 6 Applying None-Plans to Find Plans
- 7 Experimental Results

# Main Contributions

- A (new?) method for improving efficiency of algorithms solving hard problems,
- A (new?) reduction method for planning,
- Application of the results in the tool PlanICS.

## Related Work

- Planning methods and tools: OWLS-Xplan, OWLS-MX, WSMO, PDDL3, PlanICS, . . . ,
- Abstraction methods [Cousot, . . . ],
- Partial order reductions [Valmari, Peled, Godefroid, . . . ],
- Symmetry reductions [Clarke, Emerson, Jha, Sistla, . . . ],
- CEGAR – Counterexample Guided Abstraction [Clarke],
- . . . and others.

## General idea – intuition

- **D** – a domain to find a **plan** (problem is NP-complete),
- **D'** – an abstract domain in which finding a **plan** is easy,
- a **plan** in **D'** does not need to correspond to a **plan** in **D** ,
- a **none-plan** in **D'** corresponds to a **none-plan** in **D** ,
- find (the) **none-plans** in **D'** ,
- prune **D** from (the) **none-plans** of **D'** ,
- search for (the) **plans** in **D** pruned.

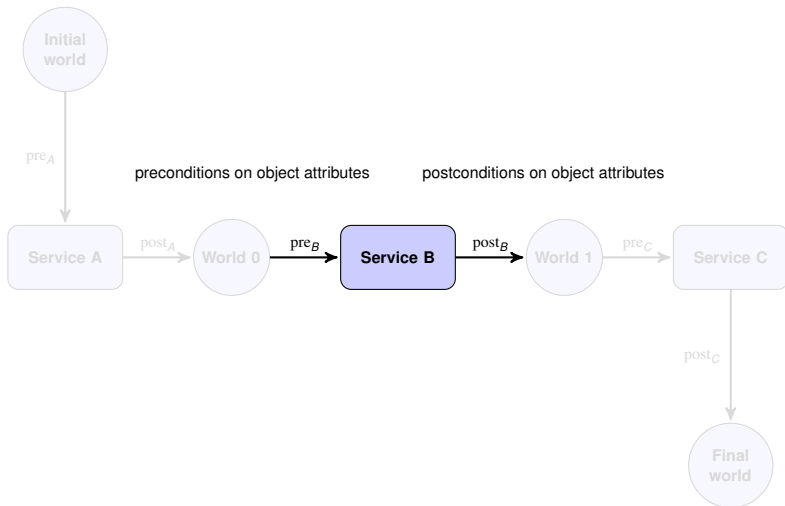
## Application to planning in PlanICS

- Given an **ontology of object types** and **services**,
- Given a user query: (**initial worlds**, **final worlds**),
- A **world** – a set of **objects** (object has a **type** and **attributes**),
- A **service**: (**in**, **inout**, **out**, **pre**, **post**), where in, inout, out are sets of objects,
- **pre** – a bool. form. over **object attributes** of in and inout,
- **post** – a bool. form. over **object attributes** of inout and out.

**Task: Find all plans from some **initial** to some **final world**.**

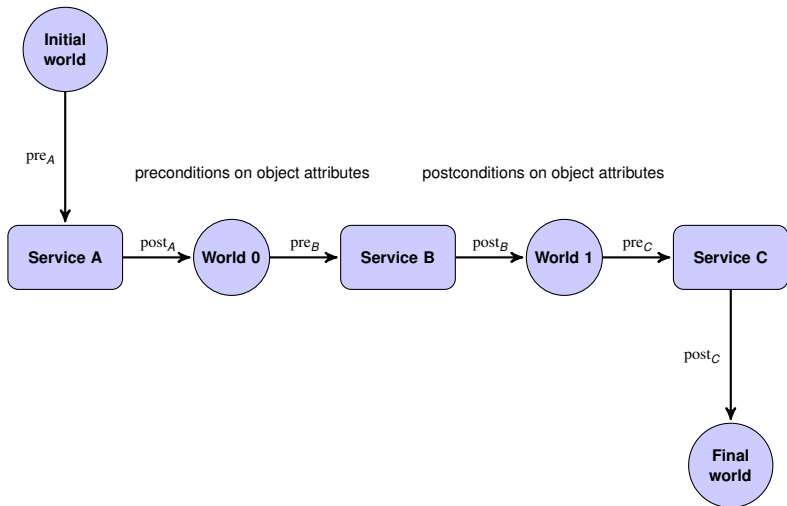
*(This problem is NP-complete.)*

# Service composition in PlanICS



Planning – composition of services (a huge number of plans)

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Planning – composition of services (a huge number of plans)



## Simplifying the planning domain

**Idea** – simplify services and worlds:

- the simplified **objects** do not have attributes,
  - a simplified **world** – a multiset of objects,
  - a simplified **service** – (**precondition**, **effect**),
  - **precondition** – a multiset of objects (objects required),
  - **effect** – a multiset of objects (new objects added).
- 
- **B** – a set of services, **B'** – the set of simplified services,
  - Fact: If **B'** cannot be composed into a plan, then **B** cannot be composed into a plan,
  - **Goal**: synthesize constraints of non-composability.

## (Simplified) Planning Domain

**(Simplified) Planning Domain**  $\mathcal{P} = (\mathcal{W}_{\mathcal{H}}, F_I, F_G, Act)$ :

- $\mathcal{W}_{\mathcal{H}} \subseteq \mathbb{N}^n$  – a set of abstract worlds (multisets),
- $F_I, F_G \subseteq \mathcal{W}_{\mathcal{H}}$  – initial, final worlds,
- $Act$  – a set of actions (simplified services).

where  $n$  is the number of all types of the objects.

For each  $act \in Act$ :

- $pre(act)$  – **precondition** of  $act$ ,
- $eff(act)$  – **effect** of  $act$ .

$pre(act), eff(act) \in \mathbb{N}^n$ .

Action  $act \in Act$  is **enabled** in  $\omega \in \mathcal{W}_{\mathcal{H}}$  iff  $pre(act) \leq \omega$  and the results of firing  $act$ :  $\omega \xrightarrow{act} \omega + eff(act)$

# Plans

Given  $\mathcal{P} = (\mathcal{W}_{\mathcal{H}}, F_I, F_G, Act)$ ,  $\mathbf{B} \subseteq Act$

- $\pi \in \Pi(\omega, \mathbf{B}, \omega')$  iff

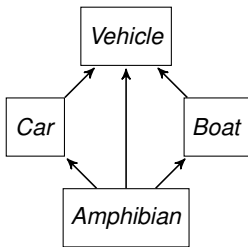
$$\pi = \omega_0 \xrightarrow{\text{act}_1} \omega_1 \xrightarrow{\text{act}_2} \dots \xrightarrow{\text{act}_{n-1}} \omega_{n-1} \xrightarrow{\text{act}_n} \omega_n$$

where  $\omega_0 = \omega$ ,  $\omega_n \geq \omega'$ , and  $\{\text{act}_1, \dots, \text{act}_n\} \subseteq \mathbf{B}$

- $\bigcup_{\omega_I \in F_I} \bigcup_{\omega_F \in F_G} \Pi(\omega_I, \mathbf{B}, \omega_F)$  – the **plans** over  $\mathbf{B}$

Each plan starts from an initial world and its last world covers a final world.

## Exemplary planning domain

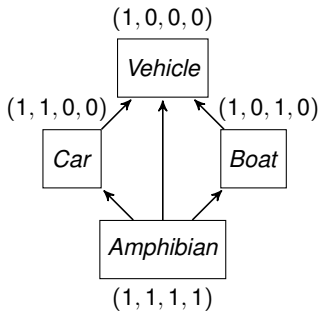


Vehicles' inheritance

### Actions:

- *makeVehicle*:  
*needs nothing, builds vehicle*
- *makeCar*:  
*needs vehicle, builds car*
- *makeBoat*:  
*needs vehicle, builds boat*
- *makeAmphibian*:  
*needs boat and car, builds amphibian*
- *tinker*:  
*needs amphibian and car, builds two amphibians*

## Exemplary planning domain, ct'd



Vehicles' inheritance

Order of the objects:

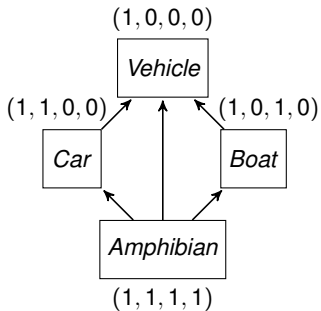
(*Vehicle, Car, Boat, Amphibian*)

- *makeAmphibian*:  
needs boat and car, builds amphibian

$$\text{pre}(\textit{makeAmphibian}) = \\ (1, 0, 1, 0) + (1, 1, 0, 0) = \\ (2, 1, 1, 0)$$

$$\text{eff}(\textit{makeAmphibian}) = (1, 1, 1, 1)$$

## Exemplary planning domain, ct'd



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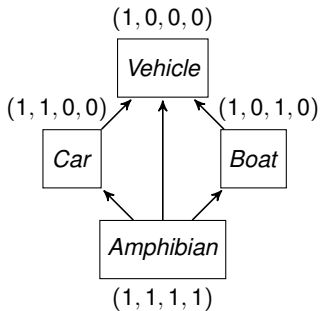
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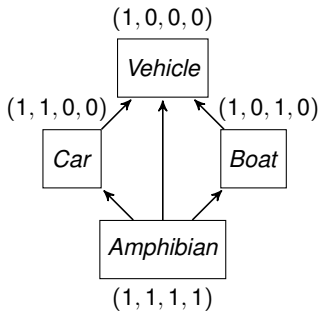
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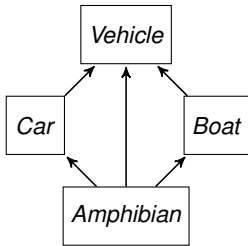
- *makeAmphibian*:  
needs boat and car, builds  
*amphibian*

$$\begin{aligned} \text{pre}(\textit{makeAmphibian}) &= \\ (1, 0, 1, 0) + (1, 1, 0, 0) &= \\ (2, 1, 1, 0) \end{aligned}$$

$$\text{eff}(\textit{makeAmphibian}) = (1, 1, 1, 1)$$



## Exemplary planning domain, ct'd



Vehicles' inheritance

### Actions:

- $\text{pre}(\textit{makeVehicle}) = (0, 0, 0, 0)$   
 $\text{eff}(\textit{makeVehicle}) = (1, 0, 0, 0)$
- $\text{pre}(\textit{makeCar}) = (1, 0, 0, 0)$   
 $\text{eff}(\textit{makeCar}) = (1, 1, 0, 0)$
- $\text{pre}(\textit{makeBoat}) = (1, 0, 0, 0)$   
 $\text{eff}(\textit{makeBoat}) = (1, 0, 1, 0)$
- $\text{pre}(\textit{makeAmphibian}) = (2, 1, 1, 0)$   
 $\text{eff}(\textit{makeAmphibian}) = (1, 1, 1, 1)$
- $\text{pre}(\textit{tinker}) = (2, 2, 1, 1)$   
 $\text{eff}(\textit{tinker}) = (2, 2, 2, 2)$

$\omega_I = (0, 0, 0, 0)$  (one initial world)

$\omega_F = (0, 0, 0, 1)$  (one final world)

## Classifying actions

$V_{\max}$  - the largest number occurring in  $\text{pre}(\text{act})$  for  $\text{act} \in \text{Act}$ .

$$\text{enact}(\mathbf{A}) = \{\text{act} \in \text{Act} \mid \sum_{\text{act}' \in \mathbf{A}} V_{\max} \cdot \text{eff}(\text{act}') \geq \text{pre}(\text{act})\}.$$

all actions that can be enabled by firing actions from  $\mathbf{A} \subseteq \text{Act}$ ,

$\omega \in \mathcal{W}_{\mathcal{H}}$ ,  $i > 0$

- $G_0^\omega = \{\text{act} \in \text{Act} \mid \text{pre}(\text{act}) \leq \omega\}$  – the actions enabled in  $\omega$ ,
- $G_{i+1}^\omega = \text{enact}(G_i^\omega)$  – the actions enabled in  $i$ -th step
- $H_0^\omega = G_0^\omega$ ,
- $H_{i+1}^\omega = G_{i+1}^\omega \setminus G_i^\omega$  – the actions **newly** enabled in  $i$ -th step.

## Classifying actions, ct'd

$\omega, \omega' \in \mathcal{W}_{\mathcal{H}}$

$$\text{kgoal}(\omega, \omega') = \min(\{k \in \mathbb{N} \mid \sum_{\text{act} \in G_k^\omega} V_{\max} \cdot \text{eff}(\text{act}) \geq \omega'\})$$

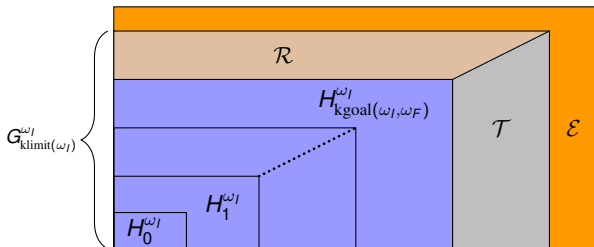
the minimal step at which greedily fired actions cover  $\omega'$ .

### Lemma A

- $\text{kgoal}(\omega, \omega') < \infty$  iff  $\Pi(\omega, \text{Act}, \omega') \neq \emptyset$ ,
- $\text{kgoal}(\omega, \omega')$  can be computed in time  $O(|\text{Act}|^2 \cdot n)$ .

Planning in  $\mathcal{P}$  is easy.

## Classifying actions, cont'd



$$\omega_I \in F_I, \omega_F \in F_G, \text{klimit}(\omega_I) = \min(\{k \in \mathbb{N} \mid H_k^{\omega_I} = \emptyset\})$$

- $\mathcal{E} = \text{Act} \setminus G_{\text{klimit}(\omega_I)}^{\omega_I}$  – **useless** actions can't be enabled
- $\mathcal{G} = G_{\text{kgoal}(\omega_I, \omega_F)}^{\omega_I}$  – **sufficient** actions can cover goal
- $\mathcal{R} = \{\text{act} \in G_{\text{klimit}(\omega_I)}^{\omega_I} \mid \text{pre}(\text{act}) \geq \omega_F\}$  – **redundant** actions
- $\mathcal{T} = G_{\text{klimit}(\omega_I)}^{\omega_I} \setminus (G_{\text{kgoal}(\omega_I, \omega_F)}^{\omega_I} \cup \mathcal{R})$  – **potentially** useful acts

## Classifying actions, cont'd

### Lemma B

Let  $A \subseteq Act$ . If there is a plan over  $A$ , then  $A$  contains at least one element from  $H_i^{\omega_I}$  for all  $0 \leq i \leq k_{goal}(\omega_I, \omega_F)$

### First easy reductions:

- throw away **redundant** (e.g., *tinker*) and **useless** actions,
- block all sets of actions that do not satisfy Lemma B.

More reductions: consider none-plans.

## None-plans

$$\mathbf{A} \subseteq \text{Act}, \omega, \omega' \in \mathcal{W}_{\mathcal{H}}$$

$$\mathcal{Z}(\omega, \mathbf{A}, \omega') := \{B \subseteq \mathbf{A} \mid \Pi(\omega, B, \omega') = \emptyset\}$$

None-plan: a set of actions  $B$ , which is not a support of a plan starting at  $\omega$  and covering  $\omega'$ .

$\mathbb{I}(\omega) := \{\omega' \mid \|\omega'\| = 1 \wedge \omega \geq \omega'\}$  – unitary coord. vects. of  $\omega$

e.g.,  $\mathbb{I}((2, 1, 1, 0)) = \{(1, 0, 0, 0), (0, 1, 0, 0), (0, 0, 1, 0)\}$

# Characterisation of none-plans

## Theorem

$$\mathcal{Z}(\omega, A, \omega') = \bigcup_{\substack{\omega'' \in \mathbb{I}(\omega') \\ \omega \not\geq \omega''}} \bigcap_{\substack{\text{act} \in A \\ \text{eff}(\text{act}) \geq \omega''}} (\mathcal{D}(\omega, A, \text{act}) \cup 2^{A \setminus \{\text{act}\}})$$

where  $\mathcal{D}(\omega, A, \text{act}) = \{B \cup \{\text{act}\} \mid B \in \mathcal{Z}(\omega, A \setminus \{\text{act}\}, \text{pre}(\text{act}))\}$

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for each action  $\text{act}$  that could cover  $\omega''$  when fired  
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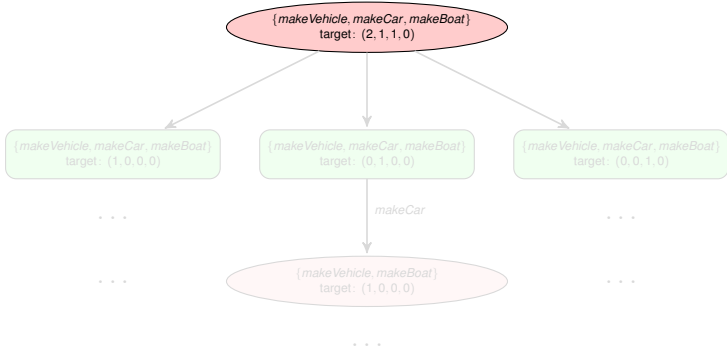
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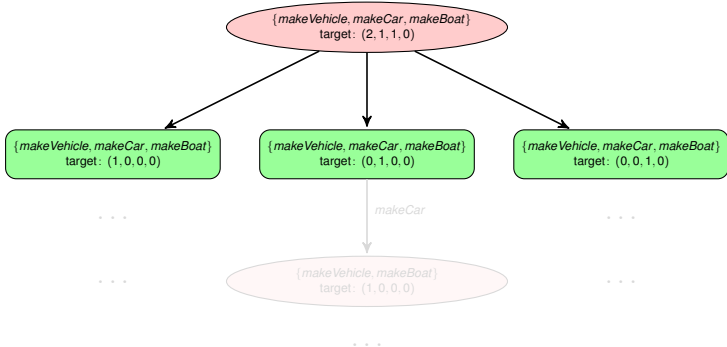


$$\mathcal{Z}((0, 0, 0, 0), \{makeVehicle, makeCar, makeBoat\}, (2, 1, 1, 0)) =$$

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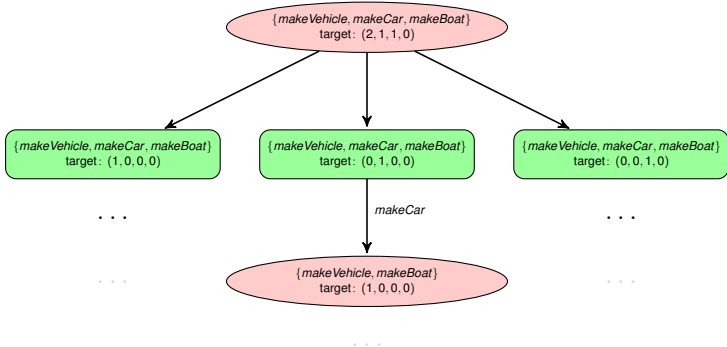


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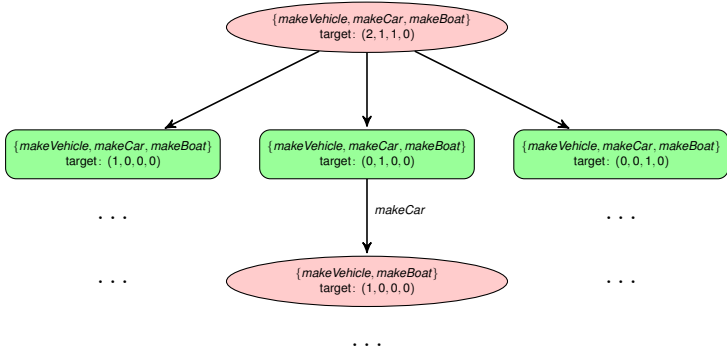
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## None-plans: the full tree unfolding

One can stop unfolding at depth  $k$  to underapproximate the none-plan space.

## Back to the original domain

SMT-formulae encoding:

- $AP$  – encoding of the **original domain** plan space (courtesy of PlanICS),
- $CL$  – blocking sets following from **Lemma B**,
- $NO\mathcal{P}^k$  – encoding of the **none-plan** space unfolding up to  $k \in \mathbb{N} \cup \{\omega\}$

A new encoding in the **original domain** plan space:

$$\widetilde{AP}^k = AP \wedge CL \wedge \neg NO\mathcal{P}^k$$

A longer formula: easier or more difficult for an SMT-solver?

# Experimental results

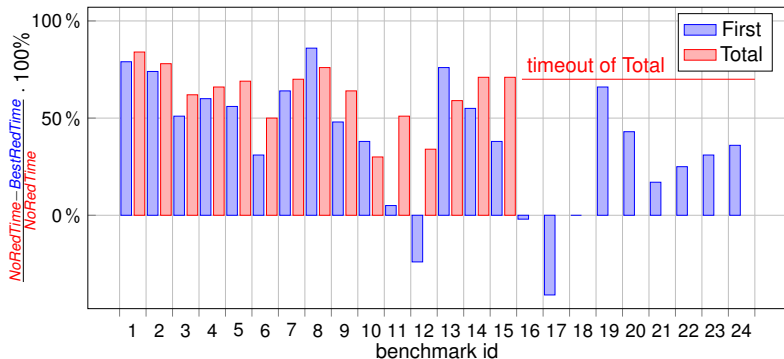
## Setup:

- random ontologies produced by Ontology Generator
- two experiments/ontology:
  - First** – single plan synthesis
  - Total** – all plan synthesis

## Results for reduction:

- **First** – **usually** substantial speedup at **some** depth
- **Total** – **always** substantial speedup at **some** depth

## Experimental results, ct'd



*NoRedTime* – time without reduction

*BestRedTime* – best time with reduction

# Conclusions

- A new method for **improving efficiency** of algorithms solving hard problems,
- A new **reduction method** for planning,
- **Application** of the results in the tool PlanICS: quite impressive improvement in some cases,
- *SEFM 2015 Best Paper Award.*

Thank you!